

Level: Grade Two

Standard: Geometry and Measurement

Learning Target: Focus on Measurement

measurement.

Checks for Understanding

0206.4.4	Estimate, measure, and calculate length to the nearest unit.
0206.4.5	Use rulers to measure the lengths of sides and diagonals of
	common 2-dimensional figures and polygons.
0206.4.6	Understand the inverse relationship between the size of a
	unit and the number of units used in a particular

Grade 2–Focus on Measurement Quilt Squares

The purpose of the Mathematics Challenges is to provide opportunities for students to develop and demonstrate understanding of important mathematical concepts and standards. Each Challenge includes a set of tasks that require higher-order thinking skills. Because these types of tasks may be new for students and they will have varying levels of understanding, the student responses will vary. The Challenges and guiding questions were designed to help teachers plan their implementation and elicit, analyze, and act on evidence of student understanding.

You will be able to choose which Mathematics Challenge Packet to implement each month, according to the learning needs of your students and your teaching context. Each packet contains all the materials necessary to implement the Mathematics Challenge including a grade-appropriate Challenge, the Mathematics Challenge Meeting Protocol, and the Guiding Questions for Analyzing Student Responses to Mathematics Challenges.

For each Challenge, you will complete a six step process of planning, implementation, and analysis and reflection.

The Mathematics Challenge Process

Stage	Step	Task	
	Step 1.	Review the Mathematics Challenge Meeting Protocol	
Planning	Step 2.	Review and solve the Mathematics Challenge prior to your Professional Learning Community (PLC) meeting. Think about your responses to the guiding questions on the Meeting Protocol	
	Step 3.	Hold your PLC meeting and discuss your responses to the Guiding Questions on the Meeting Protocol	
Implementation	Step 4.	Implement the Mathematics Challenge with your class	
	Step 5.	For your own planning and documentation, respond to the Guiding Questions on the Analyzing Student Responses Protocol	
Analysis and Reflection	Step 6.	To help us improve the Challenges and to provide recommendations for teachers implementing them in future years, complete the Mathematics Challenge Feedback Log and provide copies of all student work to the Assessment Coordinator	

Grade 2–Focus on Measurement Quilt Squares

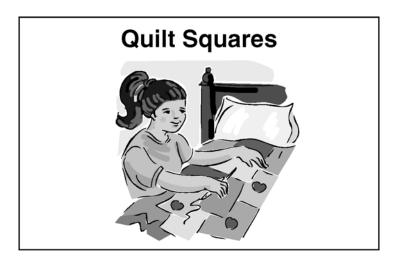
Mathematics Challenge Meeting Protocol

Each month, your Professional Learning Community will meet to discuss the implementation of one Mathematics Challenge. In preparation for your monthly meeting, please print and review this month's Mathematics Challenge, solve all tasks within the Challenge, and think about the guiding questions below. These questions will be used to facilitate a group discussion regarding the implementation of the upcoming Mathematics Challenge.

Guiding Questions for Implementing the Mathematics Challenges

- 1. What is the title of the Challenge that you will use this month?
- 2. What skills or standards is this Challenge measuring?
- 3. Where does this Challenge fit within your curriculum? Within which unit?
- 4. At what point during the unit will you administer this Challenge (e.g., At the beginning of a unit to determine what students do or do not know, at the end of a unit to assess what students have or have not learned, in the middle of a unit to determine where to go next instructionally)?
- 5. How will your students complete this Challenge (e.g., individually, one-on-one, in small groups, as a class)? Why?
- 6. Are there any prerequisite skills, common misunderstandings, or vocabulary needs that you will have to address? What are they?
- 7. What difficulties do you anticipate your students will have with the Challenge? How will you address them?
- 8. Are these skills and difficulties different for special needs students, ELL students, etc.? How? Will you do anything different for these students? What?
- 9. How will you evaluate student responses (e.g., grade responses with the provided rubric, scan responses to identify common mistakes/misconceptions, have students evaluate one another's responses, have students evaluate their own response)?
- 10. What will student responses to this Challenge tell you about student understanding?
- 11. How might you use this evidence of student understanding to adapt your teaching and learning?
- 12. What other materials, resources, or support might you need? Where can you get them?
- 13. How can your colleagues assist you in the analysis of student understanding?
- 14. What other questions or concerns do you have about this Mathematics Challenge?

After you have implemented the challenge with your class, be sure to respond to the Guiding Questions on the Analyzing Student Responses Protocol.



Standard: Geometry and Measurement

Learning Target: Focus on Measurement

Claims:

Students should understand and be able to explain or demonstrate how to:

- ✓ Estimate, measure, and calculate length to the nearest unit;
- ✓ Use rulers to measure the lengths of sides and diagonals of common 2-dimensional figures and polygons;
- ✓ Understand the inverse relationship between the size of a unit and the number of units used in a particular measurement.

Task Preparation:

Each student will need copies of the Student Response Sheet, a copy of the 4 Design Sheets at the end of the challenge, a pencil, and a ruler (inches).

Stimulus Cards (Drawing or Word Description):

Each student should have a copy of the 4 Design Sheets at the end of the challenge.

Manipulatives/Supplies:

Copies of the Student Response Sheet and the 4 Design Sheets Pencils Rulers (inches)

Cues/Directions:

Distribute student response sheets. Students should be directed to look carefully at each figure. Allow students time to answer.

- 1. Instruct students to follow along as you read aloud and say: The students in Ms. Arroyo's art class are creating designs to use as patterns for a quilt. The designs are made of squares and diagonals. Look at Design A. Use your ruler to measure the following to the nearest inch. The length of one side of the big square is "blank" inches. (TEACHER NOTE: Students should write their correct answer on the line.) The length of one side of the shaded square is "blank" inches. (TEACHER NOTE: Students should write their correct answer on the line.). If you measure one side of the shaded square in centimeters, will the answer be a number that is greater than, less than, or equal to the number you got when you measured in inches? (TEACHER NOTE: Have students check the correct box.) How do you know? (TEACHER NOTE: Students should write their explanation in the box.)
- 2. Look at Design B. Without measuring, do you think the dashed diagonal line is longer, shorter, or equal to the length of one side of the square? (TEACHER NOTE: Have students check the correct box.) How do you know? (TEACHER NOTE: Students should write their explanation in the box.)
- 3. Use your ruler to measure one side of the square in Design B. How many inches long is one side? (TEACHER NOTE: Students should write their correct answer on the line.) Now use your ruler to measure the dashed diagonal in Design B to the nearest inch. About how many inches long is the diagonal? (TEACHER NOTE: Students should write their correct answer on the line.) Is your actual measurement of the diagonal a little greater, a little less, or exactly this number? (TEACHER NOTE: Have students check the correct box.)
- 4. Look at Design C. Use your ruler to measure one side of a small square in Design C. How many inches long is one side? (TEACHER NOTE: Students should write their correct answer on the line.) Now use your ruler to measure the dashed diagonal in Design C to the nearest inch. About how many inches long is the diagonal? (TEACHER NOTE: Students should write their correct answer on the line.) Is your actual measurement of the diagonal a little greater, a little less, or exactly this number? (TEACHER NOTE: Have students check the correct box.)

- 5. Now look at Design D. Use your ruler to measure one side of one of the <u>smallest</u> squares in design D. How many inches long is one side? (TEACHER NOTE: Students should write their correct answer on the line.) Now use your ruler to measure the dashed diagonal in Design D to the <u>nearest inch</u>. <u>About</u> how many inches long is the diagonal? (TEACHER NOTE: Students should write their correct answer on the line.) Is your actual measurement of the diagonal a little greater, a little less, or exactly this number? (TEACHER NOTE: Have students check the correct box.)
- 6. In Design D, if you put 2 diagonals together to make a line, how long do you think that line would be? (TEACHER NOTE: Students should write their correct answer on the line.) Why do you think that? (TEACHER NOTE: Students should write their explanation in the box.)



1

Student Response Sheet Quilt Squares

ame.	Date
	The students in Ms. Arroyo's art class are creating designs to use as patterns for a quilt. The designs are made of squares and diagonals.
	1. Look at Design A.
	a. Use your ruler to measure the following to the <u>nearest</u> <u>inch</u> .
	The length of one side of the <u>big</u> square is
	inches.
	The length of one side of the <u>shaded</u> square is
	inches.

b. If you measure one side of the shaded square in centimeters, will the answer be a number that is greater than, less than, or equal to the number you got when you measured in inches?				
	Greater than			
Check one:	Less than			
	Equal to			
How do you know?				

2.	2. Look at Design B. <u>Without measuring</u> , do you think dashed diagonal line is longer, shorter, or equal to t length of one side of the square?		
			Longer
	Check one:		Shorter
			Equal
	How do you know?		



3.	Use your ruler to measure one side of the square in Design B. How many inches long is one side?		
	inches		
	Now use your ruler to measure the dashed diagonal in Design B to the nearest inch.		
	About how many inches long is the diagonal?		
	IIICHES		
	Is your actual measurement of the diagonal a little greater a little less, or exactly this number?		

A little greater

A little less

Exactly

Check one:



4.	Look at Design C. Use your ruler to measure one side of a small square in Design C. How many inches long is one side?			
	inches			
	Now use your ruler to measure the dashed diagonal in Design C to the <u>nearest inch</u> .			
	About how many inches long is the diagonal?			
	inches			
	Is your actual measurement of the diagonal a little greater, a little less, or exactly this number?			
	A little greater Check one: A little less			
	Exactly			

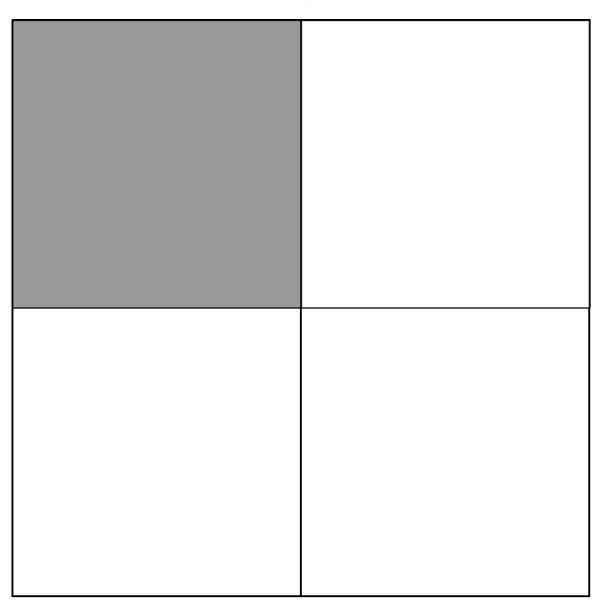


5.	Now look at Design D. Use your ruler to measure one side of one of the <u>smallest</u> squares in design D. How many inches long is one side?		
	inches		
	Now use your ruler to measure the dashed diagonal in Design D to the <u>nearest inch</u> .		
	About how many inches long is the diagonal?		
	inches		
	Is your actual measurement of the diagonal a little greater, a little less, or exactly this number?		
	A little greater		
	Check one: A little less		
	Exactly		

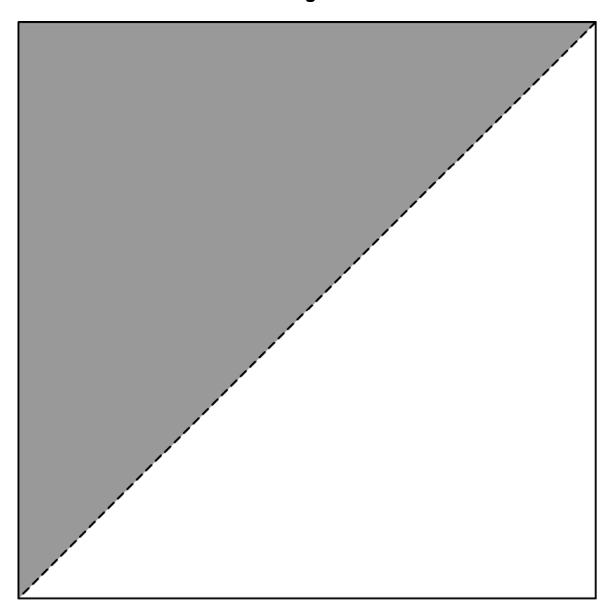


In Design D, if you put 2 diagonals together to make a line how long do you think that line would be?		
	inches	
Why do you think	that?	

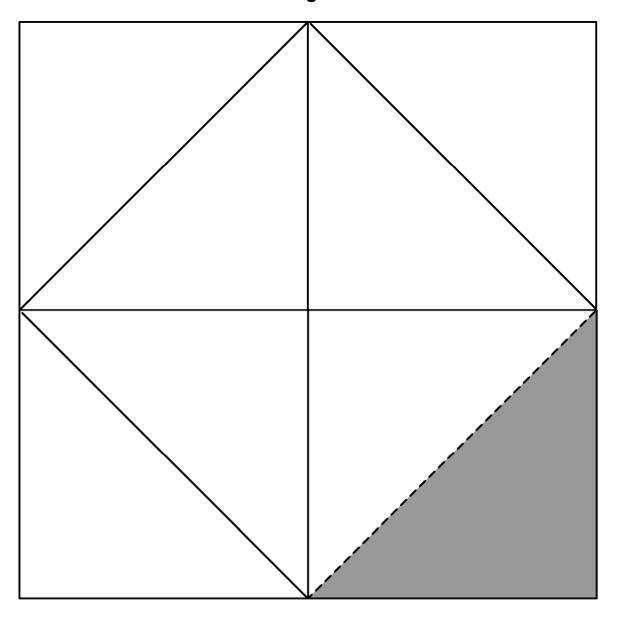
Design A



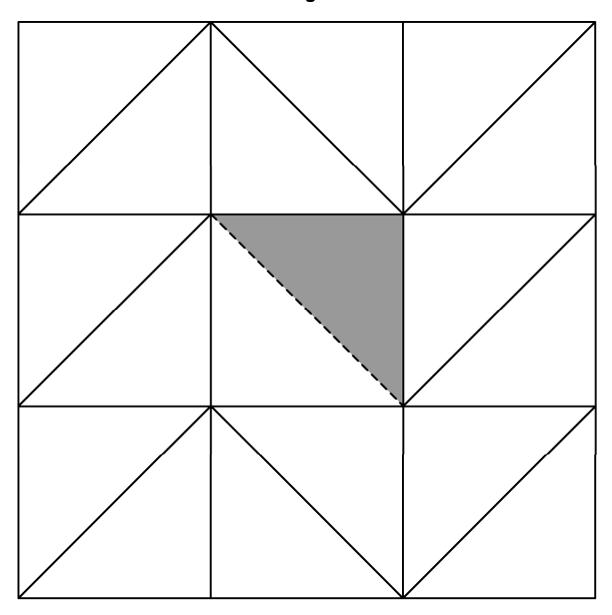
Design B



Design C



Design D



Learning and Teaching Considerations

Task 1:

- **A)** Be sure that students understand that measurement is a number that indicates a comparison between the attribute of the object (or situation or event) being measured and the same attribute of a given unit of measure. Lengths are compared to units of length in this Challenge.
- **B**) Be sure that students understand that to measure means that the attribute being measured is filled or covered or matched with a unit of measure with the same attribute. In this Challenge the attribute is length.
- C) If a student says or writes, "I just know," prompt him or her by saying something like "I'm glad you know, but it's important in math to be able to explain your answers so other people can understand what you're thinking."
- **D)** If a student says or writes, "I don't know," say something positive like "Let's start with what you do know about this problem." Students often know more than they think or say, and encouraging them to vocalize or write about that knowledge is all they need.
- **E**) Be sure that students have opportunities to become familiar with the unit of measure for the task in a hands-on way. Meaningful measurement and estimation of measurements depend on a personal familiarity with the unit of measure being used.
- **F)** Be sure that students understand that inches and centimeters are standard units. Teachers can encourage students to explore different rulers and discuss why inches and centimeters are the same everywhere. Students may explain that the length of an inch and the length of a centimeter were the same on every ruler they explored. Students may explain that people have agreed how long an inch and a centimeter are.
- **G)** Students may explain that a centimeter is shorter in length than an inch. Therefore, a given length would be more centimeters long than inches long.

Task 2:

A) Be sure that students become familiar with the use of approximate language for estimating, such as about, a little less than, and a little more than. The use of approximate language is very useful because many measurements do not result in whole numbers.

B) Be sure that students begin to develop the idea that all measurements include some error but smaller units produce a greater degree of precision, or less error. For example, centimeters are more precise than inches.

Task 3:

- **A)** To help increase familiarity with units, prevent errors, and to aid in the meaningful use of measurement, be sure that students become familiar with the development of benchmarks for frequently used units of measure.
- **B)** Students should be encouraged to perform the task both procedurally and with conceptual understanding. They should be given opportunities to discuss the concept of measuring as a process of comparing attributes as well as opportunities to use measuring units and measuring instruments.

Task 4:

A) Students may have the misconception that, when measuring, it isn't necessary to line up the end of the ruler with the end of the object being measured.

Task 5:

A) Students may have the misconception that they count the first line at the end of the inch ruler in the total number of inches (which would give an answer of one extra inch). They may not realize that each inch is the distance from one point to another point.

Task 6:

A) Students may double the measurement of one diagonal by adding the measurement to itself or multiplying it by 2.

Name	: ANSWER KEY Date:
	The students in Ms. Arroyo's art class are creating designs to use as patterns for a quilt. The designs are made of squares and diagonals.
	1. Look at Design A.
	a. Use your ruler to measure the following to the <u>nearest</u> <u>inch</u> .
	The length of one side of the <u>big</u> square is
	inches.
	The length of one side of the shaded square is
	inches.
è	WITHOUT SCALING TO BE PRINTED WITHOUT SCALING TO BETAIN THESE

ADJUST ALL ANSWERS ACCORDINGLY.

b. If you measure one side of the shaded square in centimeters, will the answer be a number that is greater than, less than, or equal to the number you got when you measured in inches?

	X	Greater than
Check one:		Less than
		Equal to

How do you know?

1 CENTIMETER IS SHORTER THAN
1 (NCH. 30 IT WILL TAKE MORE
COVER THE LENGTH OF ONE SIDE.

NOTE: STUDENT IS NOT
EXPECTED TO ACTUALLY MEASURE
(N CENTIMETERS.

2. Look at Design B. <u>Without measuring</u>, do you think the dashed diagonal line is longer, shorter, or equal to the length of one side of the square?

	X Longer SEE
Check one:	Shorter
	Equal

HOUTE! THIS ASKS WHAT THE STUDENT (S THINKING, SO ANT BOX COULD BE HOW do you know?

START AT ONE END OF THE
DIAGONAL. IT TAKES Q SIDES OF
THE SOURCE TO REACH THE OTHER
END OF THE DIAGONAL. SO I SIDE
MUST BE LESS THAN THE DIAGONAL.
NOTE: THIS IS A HIGH-LEVEL RESPONSE
THAT USES DISTANCE BETWEEN &
POINTS, ANOTHER APPROACH WOULD BE
TO IMAGINE THE DIAGONAL ROTATED
HORIZONTALLY TO LINE UP WITH
THE BASE OF THERQUARE & TO
COMPARE LENGTHS, (OR VERTICALLY TO



3.	Use your ruler to measure one side of the square in
	Design B. How many inches long is one side?

_____ inches

Now use your ruler to measure the dashed diagonal in Design B to the <u>nearest inch</u>.

About how many inches long is the diagonal?

8 (029?) inches

Is your actual measurement of the diagonal a little greater, a little less, or exactly this number?

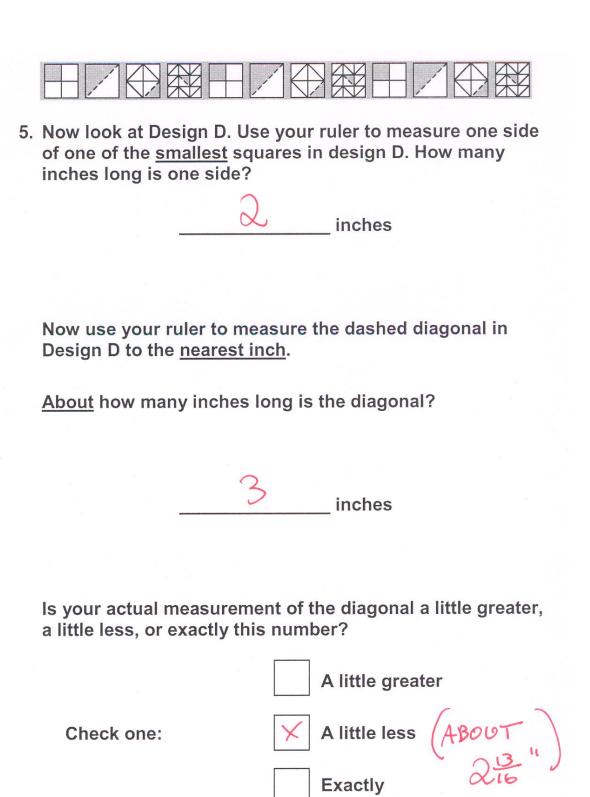
THE DIAGONAL IS JUST UNDER 85 INCHES,

Check one:

ANSWERS 9 Exactly

HINDRHIOR HINDR

4.	Look at Design C. Use your ruler to measure one side of a <u>small</u> square in Design C. How many inches long is one side?
	2
	inches
	Now use your ruler to measure the dashed diagonal in Design C to the <u>nearest inch</u> .
	About how many inches long is the diagonal?
	inches
	Is your actual measurement of the diagonal a little greater, a little less, or exactly this number?
	(ABOUT 44)
	× A little greater
	Check one: A little less
	Exactly



6. In Design D, if you put 2 diagonals together to make a line, how long do you think that line would be?

> A LITTLE LESS THAN 6 inches 52 ARE ALSO 6000 ESTIMATES

Why do you think that?

3 + 3 = 6THE ACTUAL LENGTH IS A LATTLE LESS THAN 3. SO A LITTLE LESS THAN 3 + A LITTLE LESS THAN 3 = A LITTLE LESS THAN 6 ANSWERS CAN VARY STUDENT MAY USE 2, INSTEAD OF 3.

2 \(\frac{1}{2} + 2 \frac{1}{2} = 5 \) OR MORE THAN 21+

MORE HAN 23= ALITTLE MORE THAN 5 FOR EXAMPLE.

CATEGORY	4	3	2	1
Mathematical concepts	Response shows complete understanding of the mathematical concepts used to solve the problem(s).	Response shows substantial understanding of the mathematical concepts used to solve the problem(s).	Response shows some understanding of the mathematical concepts needed to solve the problem(s).	Response shows very limited understanding of the underlying concepts needed to solve the problem(s), OR the response is not written.
	Response shows evidence in ALL of the following tasks.	Response shows evidence in only 4 of the tasks described in category 4. Student may use fractional estimates for the diagonals in tasks 3, 4, and 5. Although the fractional answer may be a correct measurement, it is not given to the nearest whole inch, as indicated in the directions.	Response shows evidence in only 3 of the tasks described in category 4.	Response shows evidence in only 2 or fewer of the tasks described in category 4.

CATEGORY	4	3	2	1
Strategy and procedures	Student typically uses an efficient and effective strategy to solve the problem(s).	Student typically uses an effective strategy to solve the problem(s).	Student sometimes uses an effective strategy to solve the problem(s), but not consistently.	Student rarely uses an effective strategy to solve the problem(s).
	Response shows evidence in ALL of the following tasks. Task 1. Teacher should indicate on response sheet if student is using ruler correctly. Student may show pencil markings on the picture of design A. Task 2. Student may show pencil markings on picture of design B. Task 3. Teacher should indicate on response sheet if student is using ruler correctly. Task 4. Teacher should indicate on response sheet if student is using ruler correctly. Task 5. Teacher should indicate on response sheet if student is using ruler correctly. Task 6. Student may show evidence of adding fractions or of drawing and measuring a line of two diagonals.	Response shows evidence in only 4 or 5 of the tasks described in category 4.	Response shows evidence in only 2 or 3 of the tasks described in category 4.	Response shows evidence in 1 or none of the tasks described in category 4.

CATEGORY	4	3	2	1
Explanation and communication	Explanation is detailed and clear; uses appropriate terminology and/or notation.	Explanation is clear; uses some appropriate terminology and/or notation.	Explanation is a little difficult to understand, but includes critical components; shows little use of appropriate terminology and/or notation.	Explanation is difficult to understand, is missing several components, and does not use or include appropriate terminology and/or notation.
	Response shows evidence in ALL of the following tasks. Task 1. Student explains that the unit centimeter is smaller than the unit inch and therefore it will take more centimeters than inches to cover the length of one side. Task 2. Student is able to give an explanation on why the diagonal is longer than one side of the square beyond saying that it looks longer. A good explanation will include distance from a starting point to an ending point. Task 6. Student explains how he or she obtained the estimate. The explanation can use the estimate from task 5 or may use addition of fractions.	Response shows evidence in only 2 explanations described in category 4.	Response shows evidence in only 1 explanation described in category 4.	Response shows no evidence of the explanations described in category 4.

CATEGORY	4	3	2	1
Mathematical accuracy	All or almost all of the steps and solutions have no mathematical errors.	Most of the steps and solutions have no mathematical errors.	Some of the steps and solutions have no mathematical errors.	Few of the steps and solutions have no mathematical errors.
	Student provides correct answers for ALL of the following tasks. Task 1. Student answers 6, 3, and checks the appropriate box, as shown on the answer sheet. Task 3. Student answers 6, 8 (or 9), and checks the appropriate box, as shown on the answer sheet. Task 4. Student answers 3, 4, and checks appropriate box, as shown on the answer sheet. Task 5. Student answer 2, 3, and checks appropriate box, as shown on the answer sheet. Task 5. Student provides an answer between 5 and 6, inclusive.	Student provides correct answers for only 4 of the tasks described in category 4.	Student provides correct answers for only 3 of the tasks described in category 4.	Student provides correct answers for 2 or fewer of the tasks described in category 4.

Scoring notes checklist

Task	Check Yes	Category
Task 1		
Student answers 6 and 3 in part (a). Students answers greater than in part (b) and explains that 1 centimeter is a shorter unit of measure than 1 inch.		Concept
Teacher should indicate on response sheet if student is using ruler correctly. Student may show pencil markings on the picture of design A.		Strategy
Student explains that the unit centimeter is smaller than the unit inch and therefore it will take more centimeters than inches to cover the length of one side.		Explanation
Student answers 6, 3, and checks the appropriate box, as shown on the answer sheet.		Accuracy
Task 2		
Student identifies the diagonal as longer without measuring it. Student also explains why it is longer without simply saying "It looks longer."		Concept
Student may show pencil markings on picture of design B.		Strategy
Student is able to give an explanation on why the diagonal is longer than one side of the square beyond saying that it looks longer. A good explanation will include distance from a starting point to an ending point.		Explanation
Task 3		
Student answers 6 and 8 or 9, as shown on the answer sheet.		Concept
(Note: An estimate of $8\frac{1}{2}$ is <u>not</u> to the nearest inch.) Student checks appropriate box.		
Teacher should indicate on response sheet if student is using ruler correctly.		Strategy
Student answers 6, 8 (or 9), and checks the appropriate box, as shown on the answer sheet.		Accuracy
Task 4		
Student answers 3 and 4, as shown on the answer sheet. (Note:		Concept
An estimate of $4\frac{1}{4}$ is <u>not</u> to the nearest inch.) Student checks		
appropriate box. Teacher should indicate on response sheet if student is using		Strategy
ruler correctly. Student answers 3, 4, and checks the appropriate box, as shown on the answer sheet.		Accuracy

Task 5	
Student answers 2 and 3, as shown on the answer sheet. (Note:	Concept
An estimate of $2\frac{7}{8}$ is <u>not</u> to the nearest inch.) Student checks	
appropriate box.	
Teacher should indicate on response sheet if student is using	Strategy
ruler correctly.	
Student answer 2, 3, and checks the appropriate box, as shown	Accuracy
on the answer sheet.	-
Task 6	
Student estimates any length between 5 and 6 inches and	Concept
provides an appropriate explanation.	1
Student may show evidence of adding fractions or of drawing and	Strategy
measuring a line of two diagonals.	
Student explains how he or she obtained the estimate. The	Explanation
explanation can use the estimate from task 5 or may use addition	
of fractions.	
Student provides an answer between 5 and 6, inclusive.	Accuracy

Analyzing Student Responses Protocol

The purpose of the Mathematics Challenges is to provide opportunities for students to develop and demonstrate understanding of important mathematical concepts and standards. They include extended responses, open-ended tasks, and tasks that require higher-order thinking skills. Because these types of tasks may be novel for students and they will have varying levels of understanding, the student responses will vary.

The guiding questions below were designed to assist you in analyzing your class' response to the Challenge and determining appropriate next steps for your teaching and learning. Responses to these questions are for your reflection and documentation and will not be collected.

Gu

idir	ng Questions for Analyzing Student Responses to the Mathematics Challenges
1.	When completing the Challenge, what did your students do well? How do you know?
2.	When completing the Challenge, what did your students struggle with? How do you know?
3.	When your students completed the Challenge, did they implement multiple correct solutions strategies? What insightful approaches to problem solving did you observe?

4.	What, if any, patterns (e.g., common errors/misconceptions) did you observe across your student responses?
5.	What questions or concerns did your students have when working through this Challenge or a particular task? Are these things you should address for the class as a whole?
6.	What, if any, feedback did you provide to your class? How did you provide it?
7.	What did you learn about your students' mathematical understanding based on their responses to this Challenge?
Remi	inders:
	After you have completed the Challenge with your class and responded to these Guiding Questions for Analyzing Student Responses, please complete the Challenge Feedback Log. A link to this Log is e-mailed to you each month. Responses will be used to improve the Challenges and to provide recommendations for teachers implementing the Challenges in future years.
2)	Please provide copies of all student work to the Assessment Coordinator.